

# Synchrotron-based High Resolution Far-infrared Spectroscopy of *trans*-butadiene

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## ELECTRONIC SUPPORTING INFORMATION

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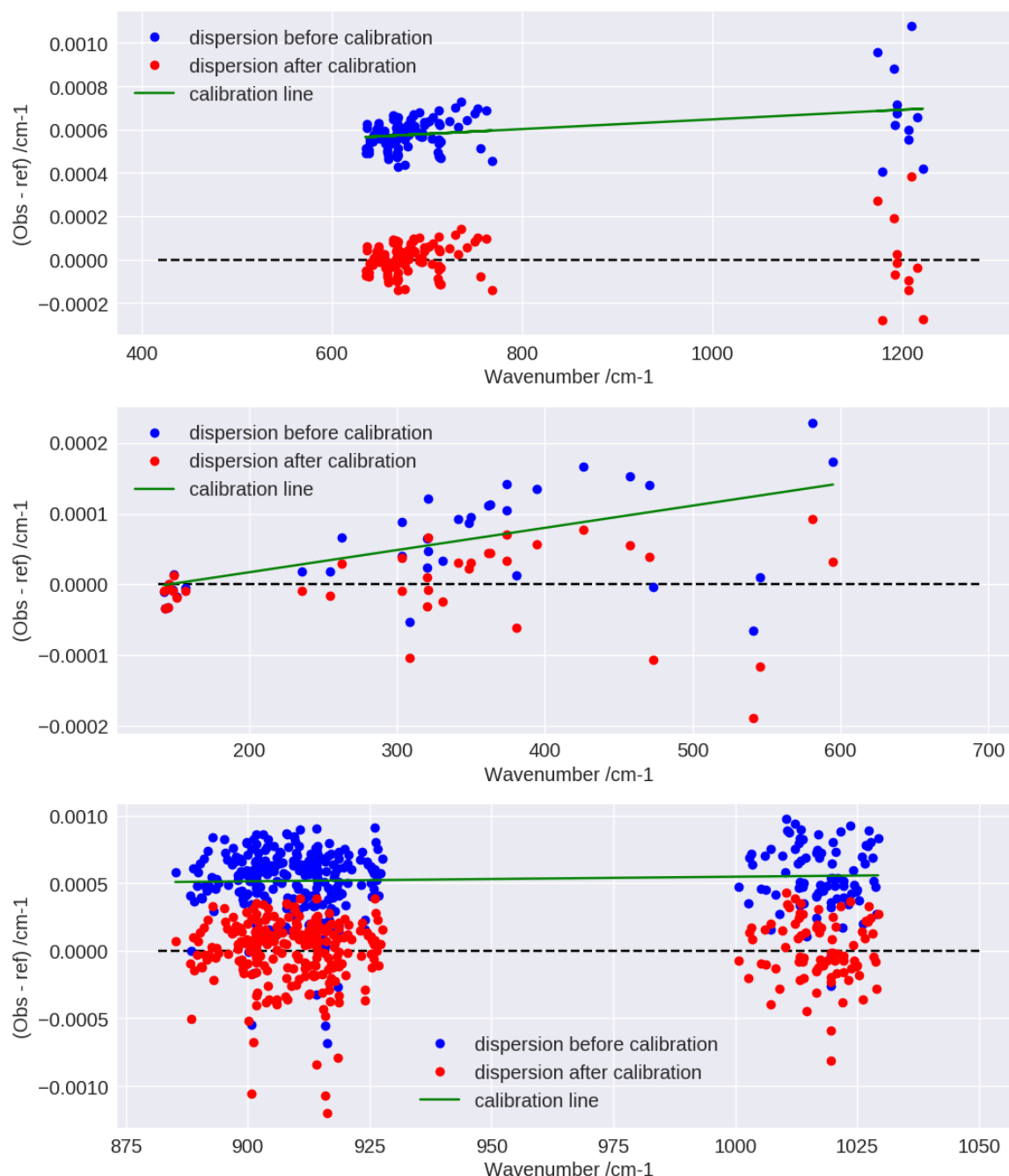
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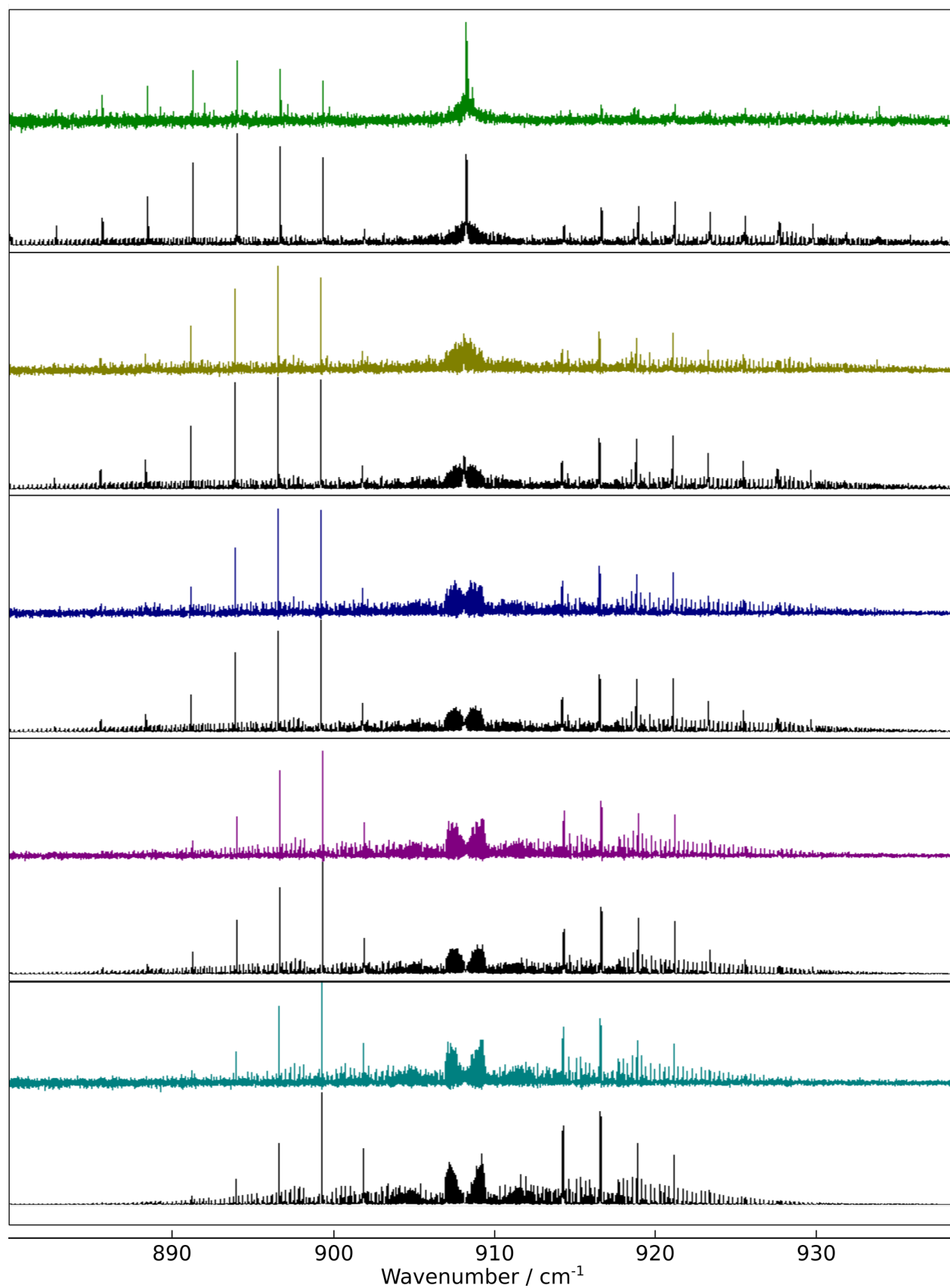
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## 1. SUPPLEMENTARY FIGURES



**Fig. S1.** Calibration plots for the warm spectrum recorded at CLS (top trace), the room temperature one recorded at SOLEIL (middle trace), and the cold spectrum recorded using the Jet-AILES apparatus at SOLEIL (bottom trace). Each dot represent the value of  $\tilde{\nu}_{\text{exp}} - \tilde{\nu}_{\text{ref}}$ , where exp refers to the experimental wavenumber and ref the accurate wavenumber used for calibration (see main text for information on reference molecules), before (in blue) and after (in red) calibration. The green lines are the calibration lines whose parameters were used to calibrate the experimental spectra. The residuals after calibration is an indication of the wavenumber accuracy one can expect from the experimental data.



**Fig. S2.** Experimental Jet-AILES spectra recorded with 0, 5, 10, 20, and 30 slm of He seeded in 2 slm of butadiene (from top to bottom, colored traced) and comparison with PGOPHER [1] simulations at temperatures of 150, 100, 70, 50, and 40 K, respectively (black traces)

## 2. SUPPLEMENTARY TABLES

**Table S1.** Calculated band centers determined at the CCSD(T)/ANO1 (“Harmonic”), hybrid harmonic/anharmonic CCSD(T)/ANO1//CCSD(T)/ANO0 (“Anharmonic”), and VPT2+K (“GUINEA”) levels of theory [2]. Intensities calculated at the harmonic CCSD(T)/ANO1 level.

$\nu$	Symmetry	Frequency / $\text{cm}^{-1}$			IR intensity / $\text{km} \cdot \text{mol}^{-1}$	
		Harmonic	Anharmonic	GUINEA	Harmonic	GUINEA
13	$a_u$	164.7543	158.1349		0.47	
24	$b_u$	289.6453	290.9936		2.16	
9	$a_g$	509.4167	504.6210		0.00	
12	$a_u$	533.9530	516.9960		11.76	
16	$b_g$	766.0941	738.7697		0.00	
8	$a_g$	895.6995	878.9920		0.00	
11	$a_u$	923.2770	884.8401		72.09	
15	$b_g$	925.1164	889.9208		0.00	
14	$b_g$	988.8452	956.5181		0.00	
23	$b_u$	994.7242	977.3987		1.24	
10	$a_u$	1042.5074	1014.1572	1012.2453	36.11	28.79
7	$a_g$	1222.3291	1194.5204		0.00	
6	$a_g$	1307.8309	1285.3375		0.00	
22	$b_u$	1310.7191	1284.7354		2.09	
21	$b_u$	1408.7609	1369.7341		4.00	
5	$a_g$	1473.3658	1428.5660		0.00	
20	$b_u$	1633.5237	1586.8279		14.39	
4	$a_g$	1695.4519	1651.6894		0.00	
3	$a_g$	3144.9188	2941.0555		0.00	
19	$b_u$	3147.1063	3038.2044		13.43	
2	$a_g$	3156.4329	3041.4562		0.00	
18	$b_u$	3162.1996	3030.8058		10.50	
1	$a_g$	3241.3186	3105.6929		0.00	
17	$b_u$	3241.5700	3106.5926		19.48	
9+12	$a_u$			1034.4503		0.22

**Table S2.** Predicted rotational constants (in  $\text{cm}^{-1}$ ) in the vibrational states of interest for this study and comparison with experimental values. Predicted values for the  $\nu_i = 1$  state have been obtained using the scaling formula  $B_{i\text{calc.}} = B_{i\text{calc.}} \times B_{0\text{exp.}}/B_{0\text{calc.}}$ .

$\nu_i = 1$	Ab initio <sup>a</sup>			Scaled			Experimental			$\delta^b$		
$i$	$A$	$B$	$C$	$A$	$B$	$C$	$A$	$B$	$C$	$\delta_A$	$\delta_B$	$\delta_C$
0	1.3674	0.1445	0.1307	–	–	–	1.3904	0.1479	0.1337			
10	1.3720	0.1435	0.1307	1.3950	0.1469	0.1337	1.3870	0.1495	0.1338	0.58	-1.75	-0.11
24	1.3233	0.1443	0.1307	1.3455	0.1478	0.1338	1.4316	0.1480	0.1336	-6.02	-0.13	0.11
9 + 12	1.3685	0.1446	0.1308	1.3915	0.1480	0.1338						

<sup>a</sup> CCSD(T)/ANO0 VPT2 (harmonic)

<sup>b</sup>  $\delta = \frac{B_{i\text{exp.}} - B_{i\text{scaled}}}{B_{i\text{scaled}}} * 100$ , in %

**Table S3.** Rotational constants and band centers (in  $\text{cm}^{-1}$ ) of butadiene after the global fit performed in this work: refit in the  $S$  reduction of all the available literature data ( $\nu_{13}$ ,  $\nu_{12}$ ,  $\nu_{11}$ ,  $\nu_{20}$ , and  $\nu_{17}$  bands) and new assignments in  $\nu_{10}$  and  $\nu_{24}$ . Brackets indicate parameters fixed to the GS values. Relevant parameters to the fit are also reported. Numbers in parenthesis are one standard deviation in units of the last quoted digit.

Constant	$\nu = 0$	$\nu_{13} = 1$	$\nu_{24} = 1$	$\nu_{12} = 1$	$\nu_{11} = 1$	$\nu_{10} = 1$	$\nu_{20} = 1$	$\nu_{17} = 1$
$E$		162.419463(12)	297.0923451(62)	524.5738512(91)	908.071968(16)	1013.368967(66)	1596.44603(88)	3100.63227(29)
$A$	1.39038236(43)	1.34477745(77)	1.43163076(55)	1.38902369(45)	1.36826885(95)	1.386966(15)	1.39260(12)	1.387928(28)
$B$	0.147885699(62)	0.147961986(77)	0.147960763(63)	0.147747042(66)	0.147738901(80)	0.14952571(74)	0.1473896(45)	0.1476913(82)
$C$	0.133694207(64)	0.134118551(80)	0.133616011(65)	0.133708028(68)	0.133725433(79)	0.13382711(68)	0.1333877(32)	0.1335834(50)
$D_J \times 10^6$	0.0287509(91)	0.030249(11)	0.0278283(90)	0.0288470(96)	0.029224(11)	0.0470(12)	0.0284(13)	[.]
$D_{JK} \times 10^6$	-0.23859(17)	-0.24946(27)	-0.24369(17)	-0.25072(18)	-0.20877(29)	-9.191(57)	-4.59(29)	[.]
$D_K \times 10^6$	7.2913(12)	-5.4398(71)	21.9587(59)	7.1452(13)	2.1983(98)	53.51(82)	[.]	[.]
$d_1 \times 10^9$	-3.5889(65)	-3.459(13)	-3.5927(71)	-3.5555(80)	-3.3252(96)	[.]	[.]	[.]
$d_2 \times 10^9$	-0.1888(25)	0.1844(60)	-0.5070(27)	[.]	[.]	[.]	[.]	[.]
$H_{JK} \times 10^9$						-6.985(70)		
$H_{KJ} \times 10^6$						0.3054(15)		
$H_K \times 10^9$			8.485(30)			434.(13)		
$L_K \times 10^{12}$			-4.010(49)					

Total	$\nu_{13}$	$\nu_{24}$	$\nu_{12}$	$\nu_{11}$	$\nu_{10}$	$\nu_{20}$	$\nu_{17}$
$N(n)^a$	10619 (9444)	1510 (1468)	2840 (1953)	2838 (2806)	2081 (2076)	764 (562)	275 (275)
$J_{\text{max}}, K_{\text{max}}^b$	88, 18	70, 10	87, 18	72, 17	72, 10	26, 7	17, 6
rms / $\text{cm}^{-1}$	0.00140	0.00033	0.00011	0.00021	0.00032	0.00075	0.00302
$\sigma^c$	1.16	1.54	1.08	1.02	1.04	1.50	1.01

<sup>a</sup> Number of lines ( $N$ ) and number of different frequencies ( $n$ ) considered in the fit (this number may differ from the number of assigned transitions, see text)

<sup>b</sup> Upper state values except in the column "Total" where the ground state values are reported <sup>c</sup> Reduced standard deviation (unitless)

**Table S4.** Transitions from the literature for which the estimated uncertainty was increased. The value used in this work is reported in the “Unc.” column. Reference to the experimental measurement is also indicated.

Band	$J'$	$K'_a$	$K'_c$	$J''$	$K''_a$	$K''_c$	Freq.	Unc.	Ref.
$\nu_{13}$	48	6	42	49	7	42	131.502667	0.002	[3]
$\nu_{13}$	35	3	32	35	2	34	171.462708	0.002	[3]
$\nu_{13}$	7	6	1	6	5	1	176.513082	0.002	[3]
$\nu_{13}$	29	5	25	28	4	25	180.853477	0.002	[3]
$\nu_{13}$	30	5	26	29	4	26	181.143133	0.002	[3]
$\nu_{13}$	63	9	54	62	8	54	198.520900	0.002	[3]
$\nu_{12}$	30	0	30	31	1	30	509.759518	0.002	[3]
$\nu_{12}$	33	3	31	32	2	31	541.217248	0.002	[3]
$\nu_{12}$	58	5	53	57	4	53	549.323537	0.002	[3]
$\nu_{12}$	56	12	44	55	11	44	568.615349	0.002	[3]
$\nu_{11}$	65	4	62	66	5	62	876.337884	0.003	[4]
$\nu_{11}$	48	0	48	47	1	46	909.847553	0.003	[4]
$\nu_{11}$	44	0	44	43	1	42	909.920503	0.003	[4]
$\nu_{20}$	37	3	35	36	3	34	1606.419508	0.07	[4]
$\nu_{20}$	38	3	36	37	3	35	1606.679400	0.07	[4]
$\nu_{20}$	39	3	37	38	3	36	1606.939468	0.07	[4]

### 3. LISTS OF ASSIGNED TRANSITIONS

All lists are reproduced in the following format:

$J' K'_a K'_c J'' K''_a K''_c$  wavenumber uncertainty  
(wavenumber and uncertainty in  $\text{cm}^{-1}$ )

Below are reported the first 100 lines of each list (by frequency order), the full lists are reported as electronic files.

#### A. $\nu_{24}$ band

##### A.1. Assigned and fitted transitions on the room temperature spectrum

The full list can be found in the file trans\_butadiene\_lin.txt where  $\nu_{24} = 1$  is coded at  $\nu = 5$ .

87	1	86	88	1	87	273.381097	0.0001
87	3	84	88	3	85	273.587850	0.0001
86	1	85	87	1	86	273.649241	0.0001
86	3	83	87	3	84	273.840097	0.0001
85	1	84	86	1	85	273.917131	0.0001
85	3	82	86	3	83	274.091812	0.0001
84	1	83	85	1	84	274.185065	0.0001
84	3	81	85	3	82	274.343286	0.0001
83	1	82	84	1	83	274.453095	0.0001
83	3	80	84	3	81	274.594412	0.0001
82	1	81	83	1	82	274.720822	0.0001
82	2	80	83	2	81	274.836181	0.0001
82	3	79	83	3	80	274.844949	0.0001
81	1	80	82	1	81	274.988684	0.0001
81	3	78	82	3	79	275.095212	0.0001
81	2	79	82	2	80	275.096833	0.0001
80	1	79	81	1	80	275.256329	0.0001
80	3	77	81	3	78	275.344857	0.0001
80	2	78	81	2	79	275.357385	0.0001
79	1	78	80	1	79	275.524066	0.0001
79	3	76	80	3	77	275.593907	0.0001
79	2	77	80	2	78	275.618045	0.0001
78	1	77	79	1	78	275.791637	0.0001
78	3	75	79	3	76	275.842199	0.0001
78	2	76	79	2	77	275.878435	0.0001
77	1	76	78	1	77	276.059155	0.0001
77	3	74	78	3	75	276.090261	0.0001
77	2	75	78	2	76	276.138788	0.0001
76	1	75	77	1	76	276.326538	0.0001
76	3	73	77	3	74	276.337707	0.0001
76	2	74	77	2	75	276.398775	0.0001
75	3	72	76	3	73	276.584181	0.0001
75	2	73	76	2	74	276.658563	0.0001
74	3	71	75	3	72	276.830003	0.0001
74	2	72	75	2	73	276.918388	0.0001
73	3	70	74	3	71	277.075368	0.0001
73	2	71	74	2	72	277.177864	0.0001
72	3	69	73	3	70	277.319876	0.0001
72	2	70	73	2	71	277.437073	0.0001
71	3	68	72	3	69	277.564034	0.0001
71	1	70	72	1	71	277.662227	0.0001
71	2	69	72	2	70	277.696161	0.0001
70	3	67	71	3	68	277.807638	0.0001
84	11	73	85	11	74	277.922049	0.0001
70	1	69	71	1	70	277.929348	0.0001
70	2	68	71	2	69	277.954923	0.0001
69	3	66	70	3	67	278.050611	0.0001
69	1	68	70	1	69	278.196057	0.0001
83	11	72	84	11	73	278.204331	0.0001
69	2	67	70	2	68	278.213303	0.0001
68	3	65	69	3	66	278.293448	0.0001
68	1	67	69	1	68	278.462838	0.0001
68	2	66	69	2	67	278.471504	0.0001
82	11	71	83	11	72	278.486327	0.0001
67	3	64	68	3	65	278.536039	0.0001
67	1	66	68	1	67	278.729378	0.0001
67	2	65	68	2	66	278.729378	0.0001
81	11	70	82	11	71	278.768557	0.0001
66	3	63	67	3	64	278.778484	0.0001
66	2	64	67	2	65	278.986606	0.0001
66	1	65	67	1	66	278.995958	0.0001
65	3	62	66	3	63	279.021110	0.0001
80	11	69	81	11	70	279.050755	0.0001
65	2	63	66	2	64	279.243568	0.0001

65	1	64	66	1	65	279.262310	0.0001
79	11	68	80	11	69	279.332789	0.0001
64	2	62	65	2	63	279.500145	0.0001
63	3	60	64	3	61	279.508204	0.0001
64	1	63	65	1	64	279.528605	0.0001
78	11	67	79	11	68	279.614955	0.0001
62	3	59	63	3	60	279.752810	0.0001
63	2	61	64	2	62	279.756200	0.0001
63	1	62	64	1	63	279.794717	0.0001
77	11	66	78	11	67	279.896906	0.0001
61	3	58	62	3	59	279.998654	0.0001
62	2	60	63	2	61	280.011813	0.0001
62	1	61	63	1	62	280.060712	0.0001
76	11	65	77	11	66	280.179226	0.0001
60	3	57	61	3	58	280.245841	0.0001
61	2	59	62	2	60	280.266794	0.0001
61	1	60	62	1	61	280.326592	0.0001
59	3	56	60	3	57	280.494620	0.0001
60	2	58	61	2	59	280.521376	0.0001
60	1	59	61	1	60	280.592208	0.0001
74	11	63	75	11	64	280.743499	0.0001
58	3	55	59	3	56	280.745272	0.0001
59	2	57	60	2	58	280.775360	0.0001
59	1	58	60	1	59	280.857797	0.0001
57	3	54	58	3	55	280.997871	0.0001
73	11	62	74	11	63	281.025208	0.0001
58	2	56	59	2	57	281.028820	0.0001
58	1	57	59	1	58	281.123188	0.0001
56	3	53	57	3	54	281.252655	0.0001
57	2	55	58	2	56	281.281772	0.0001
72	11	61	73	11	62	281.307384	0.0001
57	1	56	58	1	57	281.388315	0.0001
55	3	52	56	3	53	281.509816	0.0001
56	2	54	57	2	55	281.534267	0.0001
71	11	60	72	11	61	281.589284	0.0001
56	1	55	57	1	56	281.653146	0.0001

#### B. $\nu_{10}$ band

##### B.1. Assigned and fitted transitions from the Jet-AILES spectrum

The full list can be found in the file trans\_butadiene\_lin.txt where  $\nu_{10} = 1$  is coded at  $\nu = 6$ .

11	7	4	12	8	4	991.253455	0.0005
11	7	5	12	8	5	991.253455	0.0005
18	6	12	19	7	12	992.110766	0.0005
18	6	13	19	7	13	992.110766	0.0005
17	6	11	18	7	11	992.339372	0.0005
17	6	12	18	7	12	992.339372	0.0005
15	6	9	16	7	9	992.804081	0.0005
15	6	10	16	7	10	992.804081	0.0005
14	6	8	15	7	8	993.041078	0.0005
14	6	9	15	7	9	993.041078	0.0005
13	6	7	14	7	7	993.279740	0.0005
13	6	8	14	7	8	993.279740	0.0005
12	6	6	13	7	6	993.521450	0.0005
12	6	7	13	7	7	993.521450	0.0005
11	6	5	12	7	5	993.765834	0.0005
11	6	6	12	7	6	993.765834	0.0005
21	5	16	22	6	16	993.882154	0.0005
21	5	17	22	6	17	993.882154	0.0005
10	6	4	11	7	4	994.013307	0.0005
10	6	5	11	7	5	994.013307	0.0005
20	5	15	21	6	15	994.111527	0.0005
20	5	16	21	6	16	994.111527	0.0005
9	6	3	10	7	3	994.263384	0.0005
9	6	4	10	7	4	994.263384	0.0005
19	5	14	20	6	14	994.344398	0.0005
19	5	15	20	6	15	994.344398	0.0005
8	6	2	9	7	2	994.516495	0.0005
8	6	3	9	7	3	994.516495	0.0005
18	5	13	19	6	13	994.579972	0.0005
18	5	14	19	6	14	994.579972	0.0005
7	6	1	8	7	1	994.772359	0.0005
7	6	2	8	7	2	994.772359	0.0005
17	5	12	18	6	12	994.816881	0.0005

17	5	13	18	6	13	994.816881	0.0005	12	7	6	13	8	6	991.023893	0.0005
6	6	0	7	7	0	995.031393	0.0005	10	7	3	11	8	3	991.486854	0.0005
6	6	1	7	7	1	995.031393	0.0005	10	7	4	11	8	4	991.486854	0.0005
16	5	11	17	6	11	995.056420	0.0005	9	7	2	10	8	2	991.723093	0.0005
16	5	12	17	6	12	995.056420	0.0005	9	7	3	10	8	3	991.723093	0.0005
15	5	10	16	6	10	995.298486	0.0005	7	7	0	8	8	0	992.207873	0.0005
15	5	11	16	6	11	995.298486	0.0005	7	7	1	8	8	1	992.207873	0.0005
14	5	9	15	6	9	995.542415	0.0005	18	4	14	19	5	14	997.020643	0.0005
14	5	10	15	6	10	995.542415	0.0005	17	4	13	18	5	13	997.287492	0.0005
13	5	8	14	6	8	995.789088	0.0005	17	4	14	18	5	14	997.287492	0.0005
13	5	9	14	6	9	995.789088	0.0005	16	4	12	17	5	12	997.543715	0.0005
12	5	7	13	6	7	996.038005	0.0005	16	4	13	17	5	13	997.543715	0.0005
12	5	8	13	6	8	996.038005	0.0005	15	4	11	16	5	11	997.797170	0.0005
11	5	6	12	6	6	996.289015	0.0005	15	4	12	16	5	12	997.797170	0.0005
11	5	7	12	6	7	996.289015	0.0005	14	4	10	15	5	10	998.049117	0.0005
10	5	5	11	6	5	996.543367	0.0005	14	4	11	15	5	11	998.049117	0.0005
10	5	6	11	6	6	996.543367	0.0005	13	4	9	14	5	9	998.301750	0.0005
9	5	4	10	6	4	996.799269	0.0005	13	4	10	14	5	10	998.301750	0.0005
9	5	5	10	6	5	996.799269	0.0005	12	4	8	13	5	8	998.555949	0.0005
8	5	3	9	6	3	997.058117	0.0005	12	4	9	13	5	9	998.555949	0.0005
8	5	4	9	6	4	997.058117	0.0005	12	4	8	12	5	8	1002.218440	0.0005
7	5	2	8	6	2	997.319480	0.0005	12	4	9	12	5	7	1002.218440	0.0005
7	5	3	8	6	3	997.319480	0.0005	13	4	9	13	5	9	1002.246310	0.0005
6	5	1	7	6	1	997.583082	0.0005	13	4	10	13	5	8	1002.246310	0.0005
6	5	2	7	6	2	997.583082	0.0005	14	4	10	14	5	10	1002.275860	0.0005
5	5	0	6	6	0	997.849521	0.0005	14	4	11	14	5	9	1002.275860	0.0005
5	5	1	6	6	1	997.849521	0.0005	19	2	17	20	3	17	1002.297620	0.0005
11	4	7	12	5	7	998.811822	0.0005	15	4	11	15	5	11	1002.305550	0.0005
11	4	8	12	5	8	998.811822	0.0005	15	4	12	15	5	10	1002.305550	0.0005
10	4	6	11	5	6	999.069676	0.0005	16	4	12	16	5	12	1002.334540	0.0005
10	4	7	11	5	7	999.069676	0.0005	16	4	13	16	5	11	1002.334540	0.0005
9	4	5	10	5	5	999.329570	0.0005	17	4	13	17	5	13	1002.360690	0.0005
9	4	6	10	5	6	999.329570	0.0005	17	4	14	17	5	12	1002.360690	0.0005
8	4	4	9	5	4	999.591535	0.0005	18	2	16	19	3	16	1002.470700	0.0005
8	4	5	9	5	5	999.591535	0.0005	17	3	15	17	4	13	1004.904400	0.0005
9	5	4	9	6	4	999.616063	0.0005	18	3	16	18	4	14	1004.942270	0.0005
9	5	5	9	6	3	999.616063	0.0005	19	3	17	19	4	15	1004.982560	0.0005
18	3	15	19	4	15	999.628566	0.0005	18	3	15	18	4	15	1004.989480	0.0005
10	5	5	10	6	5	999.641418	0.0005	20	3	18	20	4	16	1005.024230	0.0005
10	5	6	10	6	4	999.641418	0.0005	19	3	16	19	4	16	1005.046270	0.0005
11	5	6	11	6	6	999.669757	0.0005	13	1	13	14	2	13	1005.109580	0.0005
11	5	7	11	6	5	999.669757	0.0005	22	3	20	22	4	18	1005.109580	0.0005
12	5	7	12	6	7	999.699703	0.0005	23	3	21	23	4	19	1005.152320	0.0005
12	5	8	12	6	6	999.699703	0.0005	17	2	15	17	3	15	1007.763860	0.0005
13	5	8	13	6	8	999.732478	0.0005	18	2	16	18	3	16	1007.879120	0.0005
13	5	9	13	6	7	999.732478	0.0005	19	2	17	19	3	17	1008.004010	0.0005
15	5	10	15	6	10	999.806160	0.0005	20	2	18	20	3	18	1008.136370	0.0005
15	5	11	15	6	9	999.806160	0.0005	19	2	17	20	1	19	1011.203580	0.0005
16	5	11	16	6	11	999.846246	0.0005	18	2	16	19	1	18	1011.441510	0.0005
16	5	12	16	6	10	999.846246	0.0005	17	2	15	18	1	17	1011.691360	0.0005
7	4	3	8	5	3	999.855708	0.0005	24	0	24	24	1	24	1013.426480	0.0005
7	4	4	8	5	4	999.855708	0.0005	25	0	25	25	1	25	1013.466850	0.0005
17	3	14	18	4	14	999.860482	0.0005	26	0	26	26	1	26	1013.504110	0.0005
17	5	12	17	6	12	999.888650	0.0005	27	0	27	27	1	27	1013.539230	0.0005
17	5	13	17	6	11	999.888650	0.0005	28	0	28	28	1	28	1013.572300	0.0005
18	5	13	18	6	13	999.934058	0.0005	29	0	29	29	1	29	1013.603200	0.0005
18	5	14	18	6	12	999.934058	0.0005	24	1	24	24	0	24	1013.809240	0.0005
19	5	14	19	6	14	999.980921	0.0005	23	1	23	23	0	23	1013.823930	0.0005
19	5	15	19	6	13	999.980921	0.0005	22	1	22	22	0	22	1013.842510	0.0005
20	5	15	20	6	15	1000.030720	0.0005	13	3	10	14	2	12	1015.666260	0.0005
20	5	16	20	6	14	1000.030720	0.0005	22	2	21	22	1	21	1015.882610	0.0005
16	3	13	17	4	13	1000.097790	0.0005	17	2	15	17	1	17	1018.998880	0.0005
6	4	2	7	5	2	1000.121710	0.0005	25	3	23	25	2	23	1019.087220	0.0005
6	4	3	7	5	3	1000.121710	0.0005	24	3	22	24	2	22	1019.174020	0.0005
15	3	13	16	4	13	1000.322940	0.0005	21	3	19	21	2	19	1019.391020	0.0005
5	4	1	6	5	1	1000.390280	0.0005	20	3	18	20	2	18	1019.447710	0.0005
5	4	2	6	5	2	1000.390280	0.0005	19	3	17	19	2	17	1019.496920	0.0005
								18	3	16	18	2	16	1019.538420	0.0005
								17	3	15	17	2	15	1019.572640	0.0005
								8	4	4	9	3	6	1019.577070	0.0005
								19	2	17	19	1	19	1019.577070	0.0005
								16	3	14	16	2	14	1019.599950	0.0005
								18	3	15	18	2	17	1020.118440	0.0005
								19	3	16	19	2	18	1020.206640	0.0005
								20	3	17	20	2	19	1020.307140	0.0005
								22	3	19	22	2	21	1020.546500	0.0005
								23	3	20	23	2	22	1020.686240	0.0005
								17	2	15	16	1	15	1021.731470	0.0005
								18	2	16	17	1	16	1022.046060	0.0005
								12	4	9	12	3	9	1022.196510	0.0005
								13	4	10	13	3	10	1022.220000	0.0005
								13	4	9	13	3	11	1022.225020	0.0005
								14	4	11	14	3	11	1022.243210	0.0005
								14	4	10	14	3	12	1022.251390	0.0005
								15	4	12	15	3	12	1022.265620	0.0005
14	7	7	15	8	7	990.574036	0.0005								
14	7	8	15	8	8	990.574036	0.0005								
12	7	5	13	8	5	991.023893	0.0005								

**B.2. Additional lines assigned in the Jet-AILES spectrum (un-fitted)**

The full list of transitions excluded from the fit is reported here in the following format:

$J' K'_a K'_c J'' K''_a K''_c$  wavenumber uncertainty  
(wavenumber and uncertainty in  $\text{cm}^{-1}$ )



17	4	14	17	3	14	1022.298830	0.0005
19	2	17	18	1	17	1022.370900	0.0005
20	2	18	19	1	18	1022.703510	0.0005
17	3	14	16	2	14	1024.462370	0.0005
18	3	15	17	2	15	1024.732760	0.0005
19	3	16	18	2	16	1024.999570	0.0005
18	3	16	17	2	16	1025.122720	0.0005
20	3	17	19	2	17	1025.263080	0.0005
22	2	21	21	1	21	1025.359170	0.0005
19	3	17	18	2	17	1025.472060	0.0005
21	3	18	20	2	18	1025.526020	0.0005
13	4	9	12	3	9	1025.887130	0.0005
13	4	10	12	3	10	1025.887130	0.0005
14	4	10	13	3	10	1026.194060	0.0005
14	4	11	13	3	11	1026.198880	0.0005
24	2	23	23	1	23	1026.306700	0.0005
15	4	11	14	3	11	1026.499950	0.0005
15	4	12	14	3	12	1026.507500	0.0005
22	3	20	21	2	20	1026.562000	0.0005
23	3	21	22	2	21	1026.938090	0.0005
17	4	13	16	3	13	1027.101830	0.0005
18	4	14	17	3	14	1027.388220	0.0005
7	7	0	7	6	2	1029.429890	0.0005
7	7	1	7	6	1	1029.429890	0.0005
8	7	1	8	6	3	1029.466880	0.0005
8	7	2	8	6	2	1029.466880	0.0005
9	7	2	9	6	4	1029.507230	0.0005
9	7	3	9	6	3	1029.507230	0.0005
10	7	3	10	6	5	1029.552100	0.0005
10	7	4	10	6	4	1029.552100	0.0005
13	7	6	13	6	8	1029.708350	0.0005
13	7	7	13	6	7	1029.708350	0.0005
14	7	7	14	6	9	1029.766060	0.0005
14	7	8	14	6	8	1029.766060	0.0005
15	7	8	15	6	10	1029.826540	0.0005
15	7	9	15	6	9	1029.826540	0.0005
16	7	9	16	6	11	1029.889820	0.0005
16	7	10	16	6	10	1029.889820	0.0005
17	7	10	17	6	12	1029.954640	0.0005
17	7	11	17	6	11	1029.954640	0.0005
18	7	11	18	6	13	1030.021240	0.0005
18	7	12	18	6	12	1030.021240	0.0005
19	7	12	19	6	14	1030.091550	0.0005
19	7	13	19	6	13	1030.091550	0.0005
20	7	13	20	6	15	1030.162590	0.0005
20	7	14	20	6	14	1030.162590	0.0005
22	5	17	21	4	17	1031.283970	0.0005
7	7	0	6	6	0	1031.400880	0.0005
7	7	1	6	6	1	1031.400880	0.0005
8	7	1	7	6	1	1031.719890	0.0005
8	7	2	7	6	2	1031.719890	0.0005
9	7	2	8	6	2	1032.042970	0.0005
9	7	3	8	6	3	1032.042970	0.0005
10	7	3	9	6	3	1032.369460	0.0005
10	7	4	9	6	4	1032.369460	0.0005
12	7	5	11	6	5	1033.032860	0.0005
12	7	6	11	6	6	1033.032860	0.0005
13	7	6	12	6	6	1033.369770	0.0005
13	7	7	12	6	7	1033.369770	0.0005
14	7	7	13	6	7	1033.709920	0.0005
14	7	8	13	6	8	1033.709920	0.0005
15	7	8	14	6	8	1034.052200	0.0005
15	7	9	14	6	9	1034.052200	0.0005
16	7	9	15	6	9	1034.397040	0.0005
16	7	10	15	6	10	1034.397040	0.0005
17	7	10	16	6	10	1034.744360	0.0005
17	7	11	16	6	11	1034.744360	0.0005
19	7	12	18	6	12	1035.444720	0.0005
19	7	13	18	6	13	1035.444720	0.0005
20	7	13	19	6	13	1035.799460	0.0005
20	7	14	19	6	14	1035.799460	0.0005
21	7	14	20	6	14	1036.153760	0.0005
21	7	15	20	6	15	1036.153760	0.0005
22	7	15	21	6	15	1036.510630	0.0005
22	7	16	21	6	16	1036.510630	0.0005

where  $v_{10} = 1$  is coded at  $v = 6$ .

7	0	7	8	1	7	1009.648040	0.0002
8	0	8	9	1	8	1009.308150	0.0002
9	0	9	10	1	9	1008.959280	0.0002
11	0	11	12	1	11	1008.229940	0.0002
12	0	12	13	1	12	1007.848580	0.0002
13	0	13	14	1	13	1007.454390	0.0002
14	0	14	15	1	14	1007.047010	0.0002
15	0	15	16	1	15	1006.626690	0.0002
16	0	16	17	1	16	1006.191460	0.0002
17	0	17	18	1	17	1005.742730	0.0002
18	0	18	19	1	18	1005.279640	0.0002
19	0	19	20	1	19	1004.803090	0.0002
20	0	20	21	1	20	1004.312970	0.0002
21	0	21	22	1	21	1003.810180	0.0002
24	0	24	25	1	24	1002.237610	0.0002
25	0	25	26	1	25	1001.696170	0.0002
26	0	26	27	1	26	1001.147820	0.0002
27	0	27	28	1	27	1000.593550	0.0002
6	0	6	6	1	6	1012.296550	0.0002
7	0	7	7	1	7	1012.352500	0.0002
8	0	8	8	1	8	1012.413040	0.0002
9	0	9	9	1	9	1012.478440	0.0002
10	0	10	10	1	10	1012.547490	0.0002
11	0	11	11	1	11	1012.619370	0.0002
12	0	12	12	1	12	1012.692660	0.0002
13	0	13	13	1	13	1012.766540	0.0002
14	0	14	14	1	14	1012.840110	0.0002
15	0	15	15	1	15	1012.912380	0.0002
16	0	16	16	1	16	1012.982450	0.0002
17	0	17	17	1	17	1013.050560	0.0002
18	0	18	18	1	18	1013.114750	0.0002
19	0	19	19	1	19	1013.175330	0.0002
20	0	20	20	1	20	1013.233010	0.0002
21	0	21	21	1	21	1013.286840	0.0002
22	0	22	22	1	22	1013.336430	0.0002
23	0	23	23	1	23	1013.382570	0.0002
24	0	24	24	1	24	1013.426390	0.0002
25	0	25	25	1	25	1013.466570	0.0002
26	0	26	26	1	26	1013.503690	0.0002
27	0	27	27	1	27	1013.538760	0.0002
28	0	28	28	1	28	1013.571370	0.0002
29	0	29	29	1	29	1013.602480	0.0002
30	0	30	30	1	30	1013.631980	0.0002
32	0	32	32	1	32	1013.687460	0.0002
33	0	33	33	1	33	1013.713990	0.0002
34	0	34	34	1	34	1013.739170	0.0002
35	0	35	35	1	35	1013.764050	0.0002
37	0	37	37	1	37	1013.813410	0.0002
38	0	38	38	1	38	1013.837460	0.0002
39	0	39	39	1	39	1013.862020	0.0002
9	1	8	10	2	8	1007.171500	0.0002
10	1	9	11	2	9	1006.958730	0.0002
12	1	11	13	2	11	1006.533940	0.0002
13	1	12	14	2	12	1006.319790	0.0002
14	1	13	15	2	13	1006.102940	0.0002
15	1	14	16	2	14	1005.881660	0.0002
17	1	16	18	2	16	1005.419750	0.0002
18	1	17	19	2	17	1005.177550	0.0002
19	1	18	20	2	18	1004.925550	0.0002
20	1	19	21	2	19	1004.663100	0.0002
21	1	20	22	2	20	1004.388500	0.0002
22	1	21	23	2	21	1004.101340	0.0002
23	1	22	24	2	22	1003.800600	0.0002
24	1	23	25	2	23	1003.486330	0.0002
25	1	24	26	2	24	1003.155700	0.0002
26	1	25	27	2	25	1002.810550	0.0002
27	1	26	28	2	26	1002.448500	0.0002
28	1	27	29	2	27	1002.069920	0.0002
29	1	28	30	2	28	1001.673920	0.0002
30	1	29	31	2	29	1001.260740	0.0002
31	1	30	32	2	30	1000.830730	0.0002
32	1	31	33	2	31	1000.383800	0.0002
34	1	33	35	2	33	999.440171	0.0002
36	1	35	37	2	35	998.436977	0.0002
37	1	36	38	2	36	997.914997	0.0002
38	1	37	39	2	37	997.381285	0.0002
39	1	38	40	2	38	996.836785	0.0002
40	1	39	41	2	39	996.282122	0.0002
41	1	40	42	2	40	995.719652	0.0002
9	1	8	9	2	8	1010.043290	0.0002
10	1	9	10	2	9	1010.136520	0.0002
11	1	10	11	2	10	1010.237740	0.0002
12	1	11	12	2	11	1010.347330	0.0002

### B.3. Assigned transitions in the warm CLS spectrum (unfitted)

The full list can be found in the file:

trans\_butadiene\_nu10\_AssignedCLS\_lin.txt

13	1	12	13	2	12	1010.464750	0.0002
14	1	13	14	2	13	1010.589600	0.0002
15	1	14	15	2	14	1010.721510	0.0002
16	1	15	16	2	15	1010.859340	0.0002
18	1	17	18	2	17	1011.152460	0.0002
19	1	18	19	2	18	1011.306260	0.0002
20	1	19	20	2	19	1011.463830	0.0002
21	1	20	21	2	20	1011.624100	0.0002
22	1	21	22	2	21	1011.786340	0.0002
23	1	22	23	2	22	1011.949560	0.0002
24	1	23	24	2	23	1012.113400	0.0002
25	1	24	25	2	24	1012.275910	0.0002
26	1	25	26	2	25	1012.436770	0.0002
27	1	26	27	2	26	1012.594730	0.0002
28	1	27	28	2	27	1012.748300	0.0002
29	1	28	29	2	28	1012.897940	0.0002
30	1	29	30	2	29	1013.041970	0.0002

## REFERENCES

1. C. Western. *J. Quant. Spectrosc. Radiat. Transfer*, **186**, 221–242 (2016).
2. CFOUR, Coupled-Cluster techniques for Computational Chemistry, a quantum-chemical program package by J.F. Stanton, J. Gauss, M.E. Harding, P.G. Szalay with contributions from A.A. Auer, R.J. Bartlett, U. Benedikt, C. Berger, D.E. Bernholdt, Y.J. Bomble, L. Cheng, O. Christiansen, M. Heckert, O. Heun, C. Huber, T.-C. Jagau, D. Jonsson, J. Jusélius, K. Klein, W.J. Lauderdale, F. Lipparini, D.A. Matthews, T. Metzroth, L.A. Mück, D.P. O'Neill, D.R. Price, E. Prochnow, C. Puzzarini, K. Ruud, F. Schiffmann, W. Schwalbach, C. Simmons, S. Stopkowitz, A. Tajti, J. Vázquez, F. Wang, J.D. Watts and the integral packages MOLECULE (J. Almlöf and P.R. Taylor), PROPS (P.R. Taylor), ABACUS (T. Helgaker, H.J. Aa. Jensen, P. Jørgensen, and J. Olsen), and ECP routines by A. V. Mitin and C. van Wüllen. For the current version, see <http://www.cfour.de>.
3. N. C. Craig and R. L. Sams. An Investigation of the Rotamers of Butadiene by High-Resolution Infrared Spectroscopy. *J. Phys. Chem. A*, **112**(49), 12637–12646 (2008). URL: <http://dx.doi.org/10.1021/jp807677y>, doi:10.1021/jp807677y.
4. N. C. Craig, J. L. Davis, K. A. Hanson, M. C. Moore, K. J. Weidenbaum, and M. Lock. Analysis of the rotational structure in bands in the high-resolution infrared spectra of butadiene and butadiene-2,3-d(2): refinement in assignments of fundamentals. *J. Mol. Struct.*, **695**, 59–69 (2004). doi:10.1016/j.molstruc.2003.11.051.